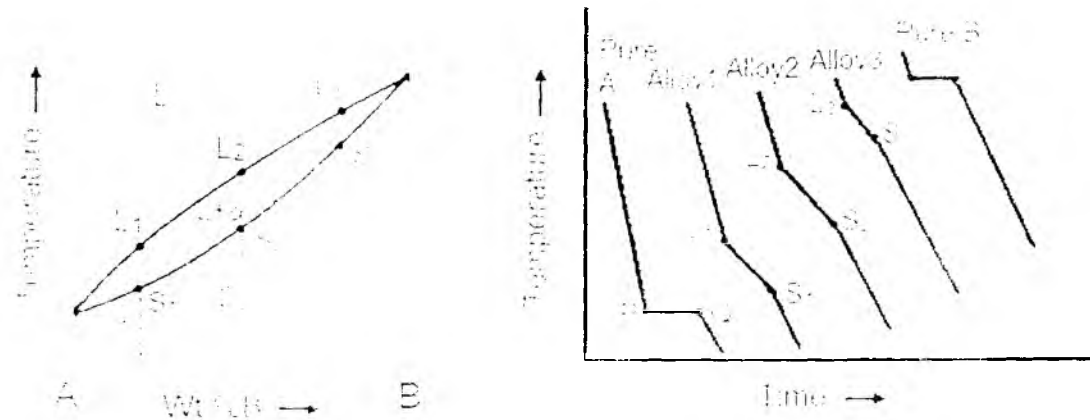


Cooling curves

- Upon cooling from liquid state, the temperature of the pure metal (A or B) drops continuously till melting point at which solidification starts. Solidification happens at a constant temperature (line PQ) as $F = 0$ ($F = 1 - 2 + 1 = 0$). The temperature drops again on completion of solidification.
- For any alloy (1, 2, 3 etc.) temp. drops till the liquidus (L_1, L_2, L_3). However, in this case, solidification proceeds over a range of temperature as $F = 1$ ($2 - 2 + 1 = 1$). Once solidification completes at the solidus (S_1, S_2, S_3) the temp. drops again.



Phase Equilibria

Simple solution system (e.g., Ni-Cu solution)

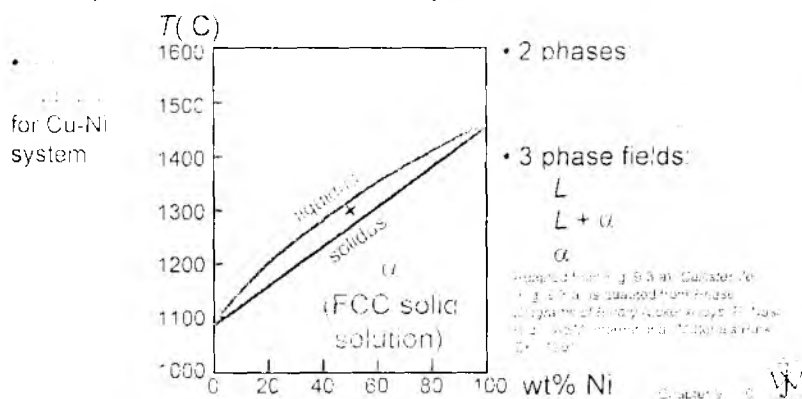
	Crystal Structure	Atomic Weight	Atomic Radius (Å)
Ni	FCC	58.7	0.1246
Cu	FCC	63.5	0.1278

- Both have the same crystal structure (FCC) and have similar electronegativities and atomic radii (V. Hume-Rothery rules) suggesting high mutual solubility.
- Ni and Cu are totally miscible in all proportions.

Chapter 9 

Phase Diagrams

- Indicate phases as function of T , C_0 , and P .
- For this course:
 - binary systems: just 2 components.
 - independent variables: T and C_0 ($P = 1$ atm is almost always used).



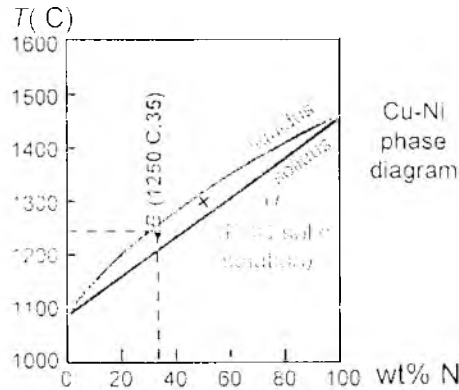
Phase Diagrams: # and types of phases

- Rule 1: If we know T and C_0 , then we know:
 - the # and types of phases present

- Examples:

At $T_B = 1250\text{ C}$, $C_0 = 45\%$
2 phases: $L + \alpha$

Adapted from Fig. 9.3.10, Callister Jr. (Fig. 9.3.10) is adapted from Phase Diagrams of Binary Nickel Alloys, P. Nash (Ed.), ASM International, Materials Park, OH, 1991.



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Phase Diagrams: composition of phases

- Rule 2: If we know T and C_0 , then we know:
 - the composition of each phase.

- Examples:

At $T_A = 1320\text{ C}$:

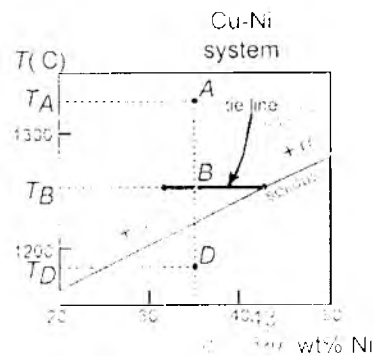
Only Liquid (L)
 $C_L = C_0$

At $T_D = 1190\text{ C}$:

Only Solid (α)
 $C_\alpha = C_0$

At $T_B = 1250\text{ C}$:

Both α and L
 $C_L = C_{\text{liquidus}}$
 $C_\alpha = C_{\text{solidus}} (= 45\text{ wt\% Ni here})$



Adapted from Fig. 9.3.10, Callister Jr. (Fig. 9.3.10) is adapted from Phase Diagrams of Binary Nickel Alloys, P. Nash (Ed.), ASM International, Materials Park, OH, 1991.

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Phase Diagrams: weight fractions of phases

- Rule 3. If we know T and C_0 then we know
--the amount of each phase (given in wt%)
- Examples:

At T_A : Only Liquid (L)

$$W_L = 100 \text{ wt\%}, W_{\alpha} = 0$$

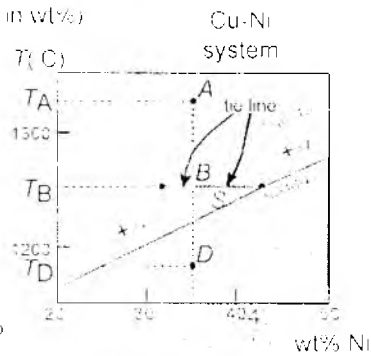
At T_D : Only Solid (α)

$$W_L = 0, W_{\alpha} = 100 \text{ wt\%}$$

At T_B : Both α and L

$$\begin{array}{r} S \\ + S \end{array} \quad \begin{array}{r} 43 - 35 \\ 43 - 32 \end{array} \quad 73 \text{ wt\%}$$

$$W_{\alpha} + S = 27 \text{ wt\%}$$

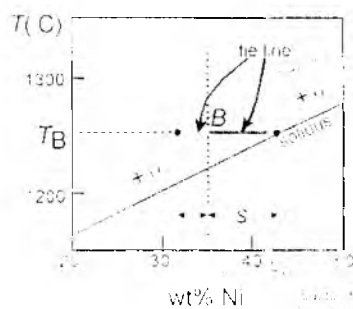


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Chapter 9

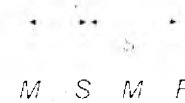
The Lever Rule

- Tie line – connects the phases in equilibrium with each other - essentially an isotherm



How much of each phase?

Think of it as a lever (teeter-totter)



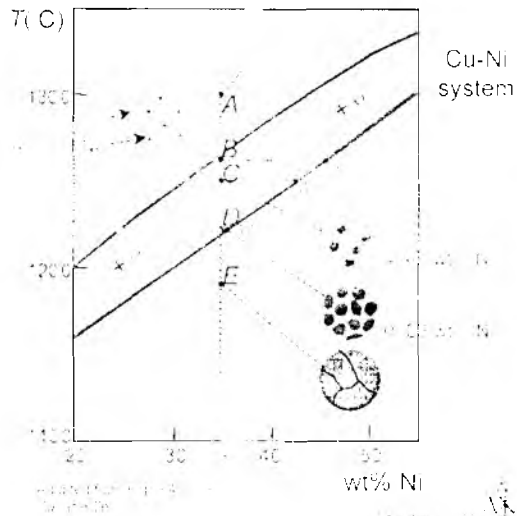
$$W = \frac{M_L}{M_L + M} = \frac{S}{R + S} = \frac{C_1 - C_0}{C_1 - C_2}$$

$$W = \frac{R}{R + S} = \frac{C_0 - C_2}{C_1 - C_2}$$

Chapter 9

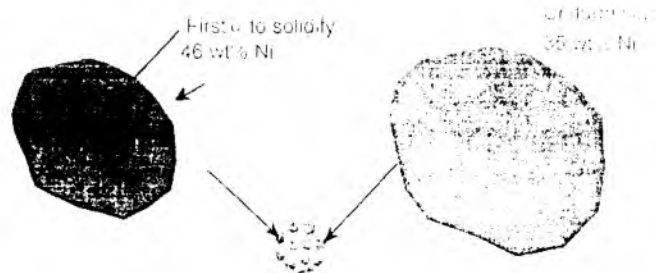
Ex: Cooling in a Cu-Ni Binary

- Phase diagram: Cu-Ni system.
- System is:
 - i.e. 2 components Cu and Ni.
 - i.e. complete solubility of one component in another; α phase field extends from 0 to 100 wt% Ni.
- Consider



Cored vs Equilibrium Phases

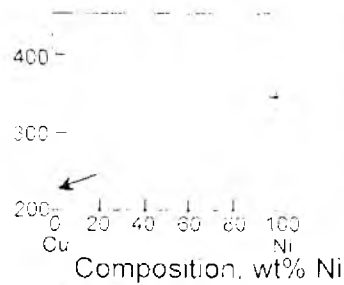
- C_{α} changes as we solidify.
- Cu-Ni case: First α to solidify has $C_{\alpha} = 46$ wt% Ni.
Last α to solidify has $C_{\alpha} = 35$ wt% Ni.
- Fast rate of cooling: Cored structure
- Slow rate of cooling: Equilibrium structure



Mechanical Properties: Cu-Ni System

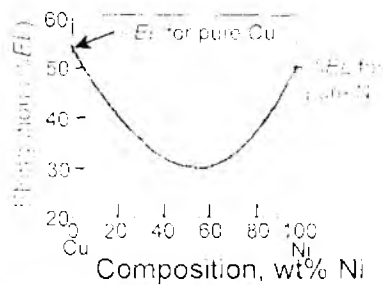
- Effect of solid solution strengthening on:

--Tensile strength (TS)



--Peak as a function of C_0

--Ductility (%EL, %AR)



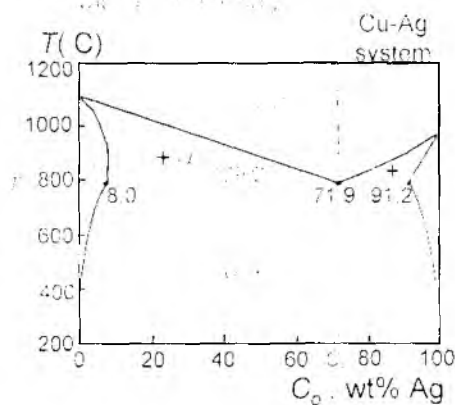
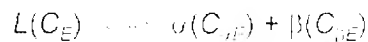
--Min. as a function of C_0

Binary-Eutectic Systems

Ex.: Cu-Ag system

- 3 single phase regions (L , α , β)
- Limited solubility:
 - α : mostly Cu
 - β : mostly Ag
- T_E : No liquid below T_E
- C_E : Min. melting T_F composition

- Eutectic transition



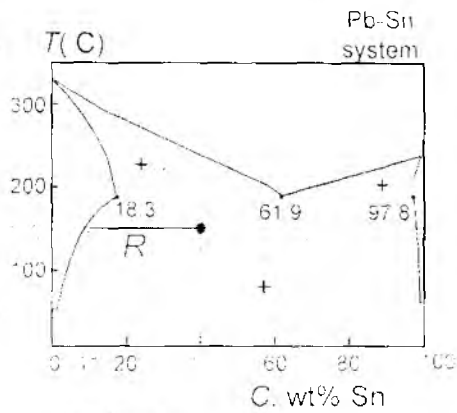
EX: Pb-Sn Eutectic System (1)

- For a 40 wt% Sn-60 wt% Pb alloy at 150 C, find...
 - the phases present: $\alpha + \beta$
 - compositions of phases

--the relative amount of each phase:

$$W_{\alpha} = \frac{C_{\beta} - C_0}{C_{\beta} - C_{\alpha}} = \frac{61.9 - 40}{61.9 - 18.3} = 21.4\%$$

$$W_{\beta} = \frac{C_0 - C_{\alpha}}{C_{\beta} - C_{\alpha}} = \frac{40 - 18.3}{61.9 - 18.3} = 78.6\%$$



Chapter 9 - 15



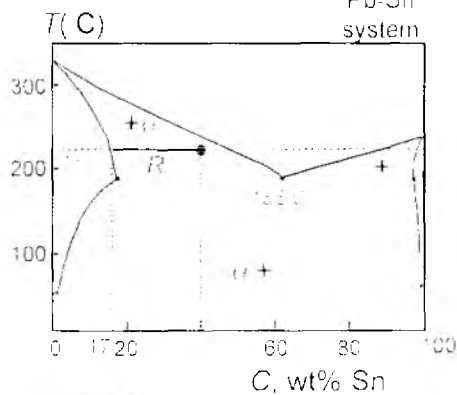
EX: Pb-Sn Eutectic System (2)

- For a 40 wt% Sn-60 wt% Pb alloy at 200 C, find...
 - the phases present: $\alpha + \beta$
 - compositions of phases:

--the relative amount of each phase:

$$W_{\alpha} = \frac{C_{\beta} - C_0}{C_{\beta} - C_{\alpha}} = \frac{61.9 - 40}{61.9 - 17.2} = 21.4\%$$

$$W_{\beta} = \frac{C_0 - C_{\alpha}}{C_{\beta} - C_{\alpha}} = \frac{40 - 17.2}{61.9 - 17.2} = 78.6\%$$

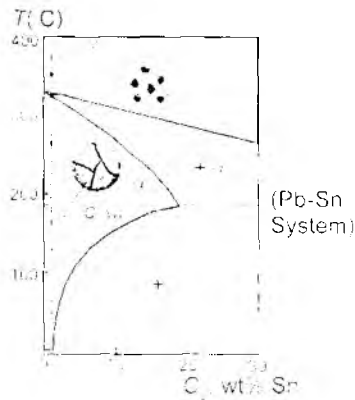


Chapter 9 - 16



Microstructures in Eutectic Systems: I

- $C_0 < 2 \text{ wt\% Sn}$
- Result:
 - at extreme ends
 - polycrystal of α grains
i.e., only one solid phase

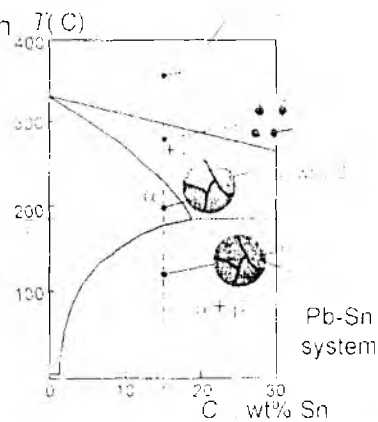


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Microstructures in Eutectic Systems: II

- $2 \text{ wt\% Sn} < C_0 < 18.3 \text{ wt\% Sn}$
- Result:
 - Initially liquid + α
 - then α alone
 - finally two phases
 - α polycrystal
 - fine β -phase inclusions

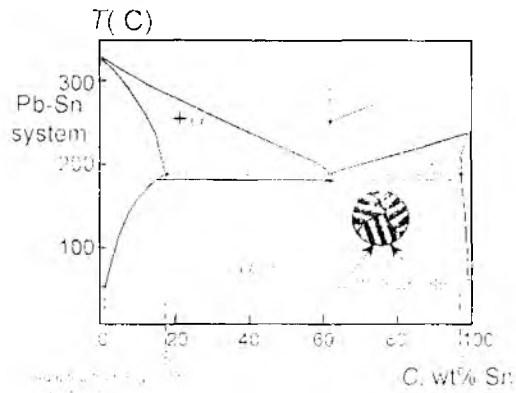


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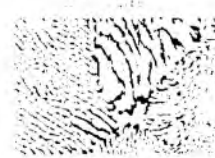
ASM

Microstructures in Eutectic Systems: III

- $C_0 = C_E$
- Result: Eutectic microstructure (lamellar structure)
 - alternating layers (lamellae) of α and β crystals



Micrograph with 67 Pb-Sn wt%



Adapted from Fig. 9.14, Callister, Jr.

Lamellar Eutectic Structure



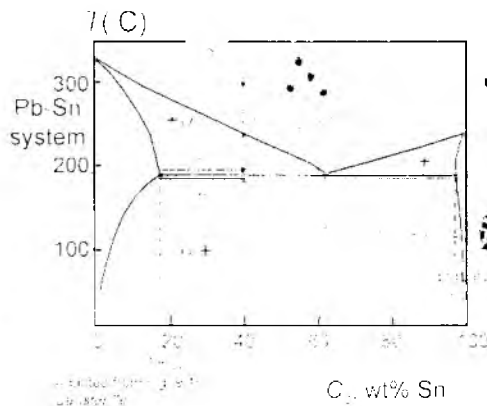
Adapted from Fig. 9.14 & 9.15, Callister, Jr.



Adapted from Fig. 9.14, Callister, Jr.

Microstructures in Eutectic Systems: IV

- 18.3 wt% Sn < C₀ < 61.9 wt% Sn
- Result: α crystals and a eutectic microstructure

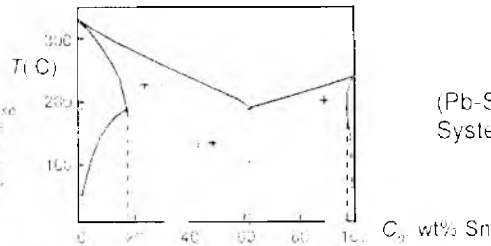


- Just above T_E
 - C_α = 18.3 wt% Sn
 - C_β = 61.9 wt% Sn
 - W_α = $\frac{C_0 - C_{\beta}}{C_{\alpha} - C_{\beta}}$ = 50 wt%
 - W_β = (1 - W_α) = 50 wt%

- Just below T_E
 - C_α = 18.3 wt% Sn
 - C_β = 97.8 wt% Sn
 - W_α = $\frac{C_0 - C_{\beta}}{C_{\alpha} - C_{\beta}}$ = 73 wt%
 - W_β = 27 wt%

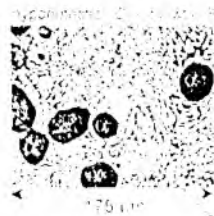
Hypoeutectic & Hypereutectic

reproduced from Fig. 8.6, Chapter 8, Fig. 8.8, and adapted from Fig. 8.9, Figure 8.10, and Fig. 8.11, in: Callias, C. J., Ed., "Materials Science and Engineering: An Introduction", 6th Edition, Wiley, 2001.



(Pb-Sn System)

reproduced from Fig. 8.11, Chapter 8, Fig. 8.11, and adapted from Fig. 8.12, Figure 8.13, and Fig. 8.14, in: Callias, C. J., Ed., "Materials Science and Engineering: An Introduction", 6th Edition, Wiley, 2001.



reproduced from Fig. 8.11, Chapter 8, Fig. 8.11, and adapted from Fig. 8.12, Figure 8.13, and Fig. 8.14, in: Callias, C. J., Ed., "Materials Science and Engineering: An Introduction", 6th Edition, Wiley, 2001.



reproduced from Fig. 8.11, Chapter 8, Fig. 8.11, and adapted from Fig. 8.12, Figure 8.13, and Fig. 8.14, in: Callias, C. J., Ed., "Materials Science and Engineering: An Introduction", 6th Edition, Wiley, 2001.



reproduced from Fig. 8.11, Chapter 8, Fig. 8.11, and adapted from Fig. 8.12, Figure 8.13, and Fig. 8.14, in: Callias, C. J., Ed., "Materials Science and Engineering: An Introduction", 6th Edition, Wiley, 2001.

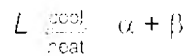
Intermetallic Compounds



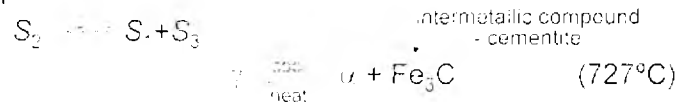
Note: intermetallic compound forms a line - not an area - because stoichiometry (i.e. composition) is exact.

Eutectoid & Peritectic

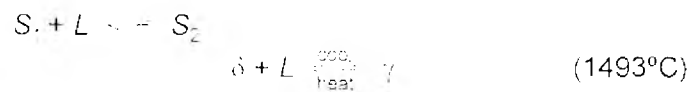
- liquid in equilibrium with two solids



$S_1 + S_2 \rightleftharpoons S_3$ - solid phase in equation with two solid phases



$S_1 + L \rightleftharpoons S_2$ - liquid + solid 1 \rightarrow solid 2 (Fig 9.21)



Eutectoid & Peritectic

Cu-Zn Phase diagram

Eutectoid phase diagram

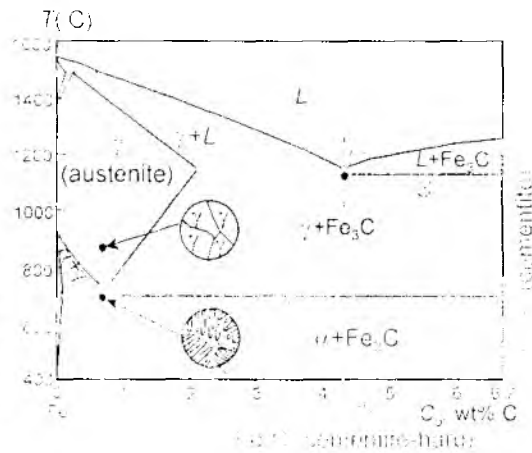
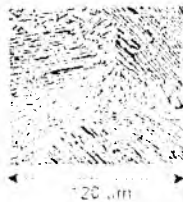
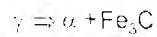
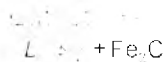
Reproduced by
Fig. 9.21 Callister 9e

Chapter 9



Iron-Carbon (Fe-C) Phase Diagram

- 2 important points



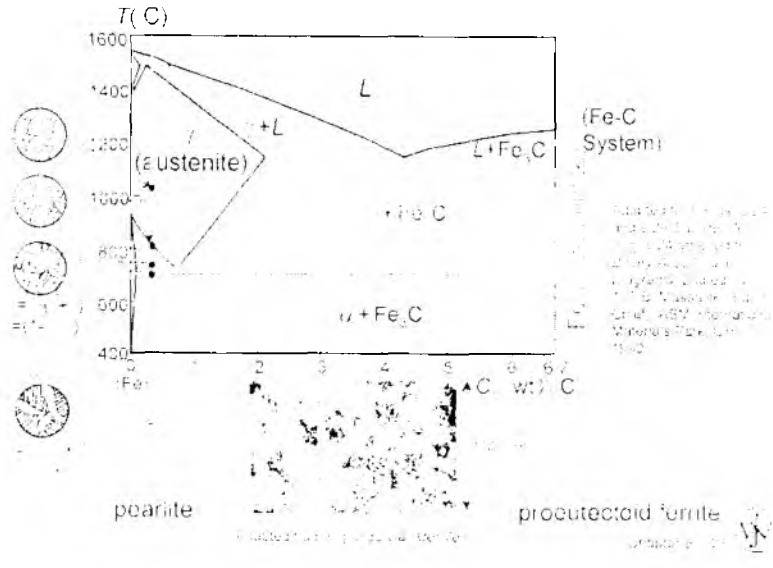
Reproduced from Fig. 9.21 Callister 9e

Reproduced from Fig. 9.21 Callister 9e

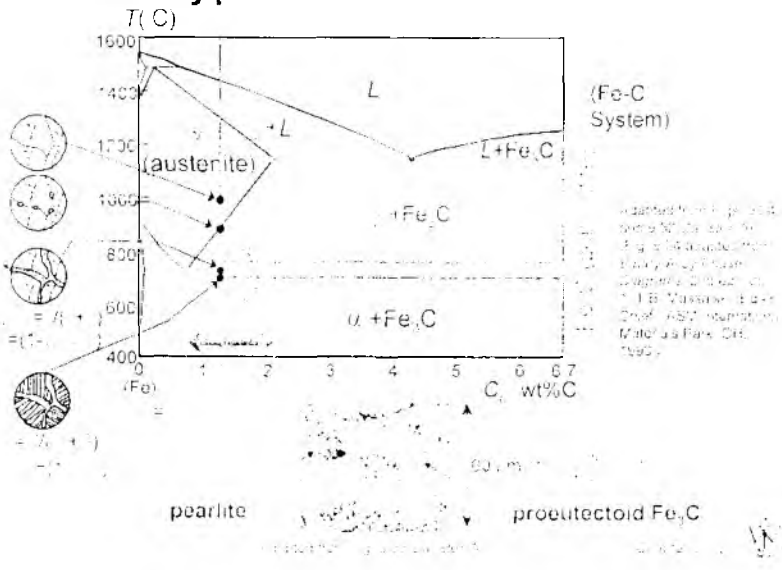
Chapter 9



eutectoid Steel



Hypereutectoid Steel



Example: Phase Equilibria

For a 99.6 wt% Fe-0.40 wt% C at a temperature just below the eutectoid, determine the following

- composition of Fe_3C and ferrite (α)
- the amount of carbide (cementite) in grams that forms per 100 g of steel
- the amount of pearlite and proeutectoid ferrite (α)

Chapter 9 -- Phase Equilibria

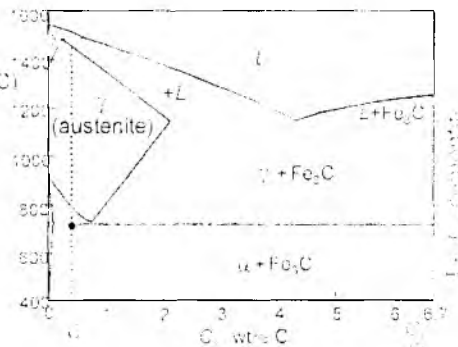
- Solution:**
- composition of Fe_3C and ferrite (α)
 - the amount of carbide (cementite) in grams that forms per 100 g of steel

$$\frac{\text{Fe}_3\text{C}}{\text{Fe}_3\text{C} + \alpha} = \frac{C_0 - C_{\alpha}}{C_{\text{Fe}_3\text{C}} - C_{\alpha}} \times 100 \quad (\text{C})$$

$$\frac{0.4 - 0.022}{6.7 - 0.022} \times 100 = 5.7\text{g}$$

$$\text{Fe}_3\text{C} = 5.7\text{g}$$

$$\alpha = 94.3\text{g}$$

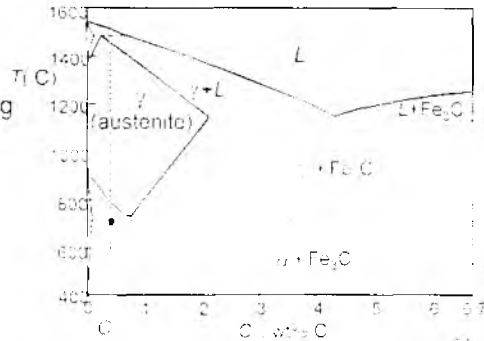


Chapter 9 – Phase Equilibria

- c. the amount of pearlite and proeutectoid ferrite (α)
 note: amount of pearlite = amount of γ just above T_e

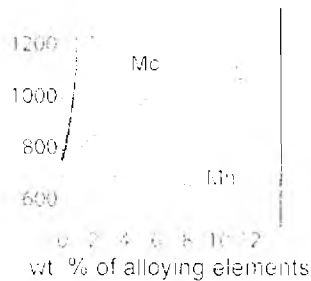
$$\frac{\gamma}{\gamma + \alpha} = \frac{C_0 - C_{\alpha}}{C - C_{\alpha}} \times 100 = 51.2 \text{ g}$$

pearlite = 51.2 g
 proeutectoid α = 48.8 g



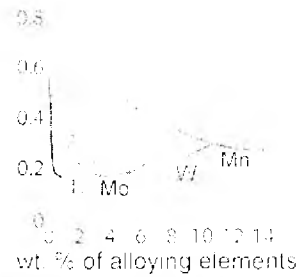
Alloying Steel with More Elements

- $T_{\text{eutectoid}}$ changes:



Revised from Fig. 9.23(a) in: Callister, T. L., and Rethwisch, D. G., Materials Science and Engineering: An Introduction, 6th Edition, Wiley-Interscience, New York, 2002, p. 717.

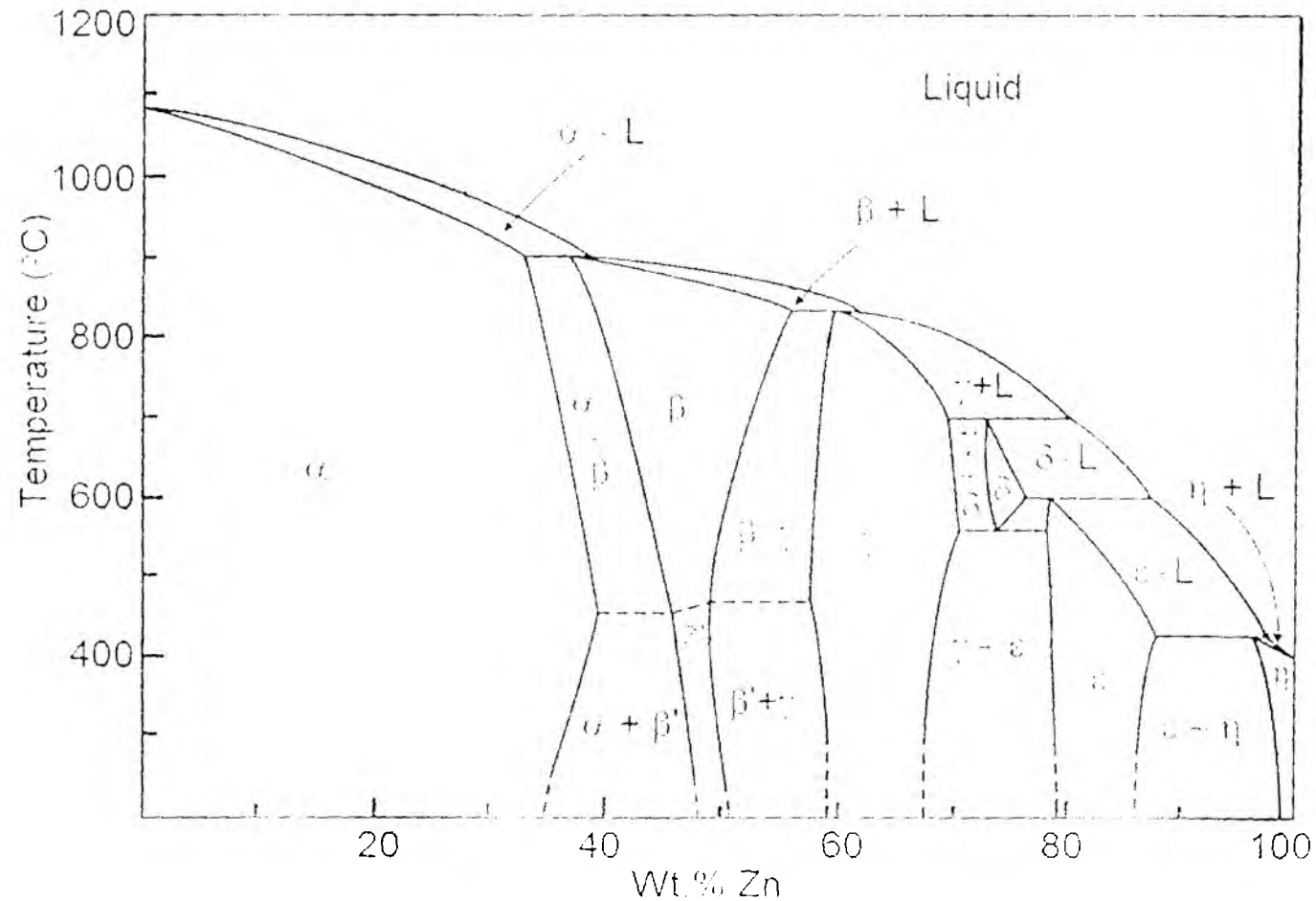
- $C_{\text{eutectoid}}$ changes:



Adapted from Fig. 9.23(b) in: Callister, T. L., and Rethwisch, D. G., Materials Science and Engineering: An Introduction, 6th Edition, Wiley-Interscience, New York, 2002, p. 717.



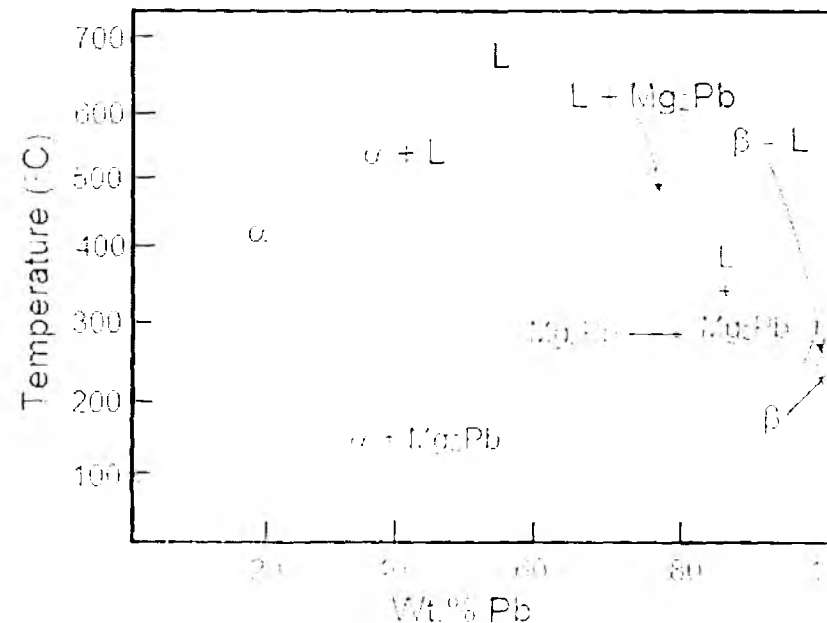
Intermediate phases - Cu-Zn Phase diagram



Cu-Zn phase diagram. α and η are terminal phases and β , γ , δ and ϵ are intermediate phases.

Phase diagrams with compounds

- Sometimes a crystalline compound called *intermetallic compound* may form between two metals.
- Such compounds generally have a distinct chemical formula or stoichiometry.
- Example – Mg_2Pb in the Mg-Pb system (appear as a vertical line at 81% Pb), Mg_2Ni , Mg_2Si , Fe_3C .



Mg - Pb phase diagram

Peritectic Phase diagram

- $L + \alpha \rightarrow \beta$. An alloy cooling slowly through the peritectic point, P , the α phase will crystallize first just below the liquidus line. At the peritectic temperature, T_P all of the liquid and α will convert to β .
- Any composition left of P will generate excess α and similarly compositions right of P will give rise to an excess of liquid.
- Peritectic systems – Pt - Ag, Ni - Re, Fe - Ge, Sn-Sb (babbitt).

