



University of Technology
Chemical Engineering Department
Mid-Year Examination – Third Class



Subject: Reactor Design

2014/2015

Branch: Chem.Proc.&Oil Ref. Branches

Examiner: Dr. Mohammad Fadhil

Time: 1 1/2 hours

Date : 26/01/2015

Q1)- Component A undergoes an irreversible isomerization liquid-phase reaction $A \longrightarrow B$, carried out in a CSTR operated adiabatically to produce 10^6 kg/year of B at 97% conversion of A. If the feed stream is to consist of pure A entering at 20°C , determine:

- Reactor volume.
- Rate of heat generation.

Additional Data

$$(x-1)(x+1) \\ x^2 - x - 1$$

Rate constant at $20^\circ\text{C} = 0.8 \text{ hr}^{-1}$; Activation energy = 2900 cal/ mole
Heat of reaction = -83 cal/g ; Molecular weight of B = Mwt of A = 250 g/gmol
The heat capacities of species A and B may be assumed to be identical and equal to $0.5 \text{ cal/g}\cdot^\circ\text{C}$. Their densities may be assumed to be equal to 0.9 g/cm^3 .

(8 Marks)

Q2) Answer one of the following questions (7 Marks)

A- A gas-phase irreversible first order reaction $A \longrightarrow R+S$ is carried out isothermally in a constant pressure batch reactor with initial conditions of $T_0=300\text{K}$, total pressure = 5 atm. The half-life of the reaction is 2 min measured at 400 K, and the heat capacity of A, R and S are 30, 25, and 20 kcal /kmol. K, respectively. Compute the time required to achieve a conversion 80% of A. The activation energy= 2 kcal/mol.

B- A solution of A is to be hydrolyzed with B solution. Two stirred tanks of equal size will be used in series setup. A and B solutions flow separately into the first tank at equal volumetric flow rates each one equal $0.004 \text{ m}^3/\text{s}$ and with concentrations of 0.02 kmol A/m^3 and 1.0 kmol B/m^3 . The reaction is:

$A + B \longrightarrow C$, the rate constant $(k) = 0.033 \text{ m}^3/\text{kmol.s}$ of the temperature at which both tanks operate. If the required conversion of A is 95%, determine

- The volume of the tanks needed.
- The space velocity of the whole system.

$$R_g = 0.082 \text{ atm.lit/gmol.K} = 1.987 \text{ cal/gmol.K}$$

Answers of Mid-Year Exam - 3rd Year 2014-2015

- A1/
- 1- Use the energy balance eqn. of adiabatic CSTR to obtain T_1 at a given $X=0.97$.

$$T_1 = \frac{C_{PA}T_0 + X(-\Delta H_R)}{C_{PA}}$$
 - 2- Apply Arrhenius eqn. to obtain K_1 at T_1 .

$$\ln \frac{K_1}{K_{293}} = \frac{E}{R} \left[\frac{1}{293} - \frac{1}{T_1} \right]$$
 - 3- Obtain $F_{A0} = \frac{F_B}{X}$; and $\dot{m}_A = F_{A0} \cdot M_{wtA}$
 and $V_0 = \frac{\dot{m}_A}{\rho}$
 - 4- $V = \frac{V_0 X}{K_1(1-X)}$
 - 5- Rate of heat generation = Rate of heat released by reaction

$$= -(-r_A)V(-\Delta H_R)$$

$$= -F_{A0}X(-\Delta H_R)$$

A2/A

- 1- Obtain K (at 400 K) by using the formula of the half-life of 1st order reaction

$$t_{1/2} = \frac{\ln 2}{K}$$

- 2- Obtain K (at 300 K) by applying Arrhenius eqn.

$$\ln \frac{K_{400}}{K_{300}} = \frac{E}{R} \left[\frac{1}{300} - \frac{1}{400} \right]$$

- 3- Determine the reaction time in a constant volume batch reactor at 300 K

$$t = \frac{1}{K} \int_0^{0.8} \frac{dx}{(1-x)(1+x)} \quad ; \quad \Sigma = y_{A0} \delta = 1(2-1) = 1$$

A2/B

- ① Set the reaction rate law:

$$(-r_A) = K C_A C_B = K C_{A0} (1-x) C_{A0} \left(\frac{C_{B0}}{C_{A0}} - x \right) \quad \text{--- (1)}$$

- ② The initial concentrations of A & B at reaction conditions,

$$C_{A0} = 0.02 \times \frac{0.004}{0.008} = 0.01 \quad \text{kmol A/m}^3$$

$$C_{B0} = 1 \times \frac{0.004}{0.008} = 0.5 \quad \text{kmol B/m}^3$$

- ③ Set material balance eqns. for CSTR1 and CSTR2 to obtain,

$$V_1 = \frac{V_0 C_{A0} X_1}{K C_{A0}^2 [(1-X_1) \left(\frac{C_{B0}}{C_{A0}} - X_1 \right)]} \quad \text{--- (2)}$$

$$V_2 = \frac{V_0 C_{A0} (X_2 - X_1)}{K C_{A0}^2 [(1-X_2) \left(\frac{C_{B0}}{C_{A0}} - X_2 \right)]} \quad \text{--- (3)}$$

- ④ Equating eqn ① and ②

$$\frac{V_1}{X_1} = \frac{V_2}{(1-X_1)(50-X_1)} = \frac{(0.95 - X_1)}{(1-0.95)(50-0.95)}$$

- ⑤ A third order eqn in X_1 is obtained which is solved to obtain X_1

- ⑥ X_1 is substituted in eqn ② or ③ to obtain V_1 or V_2

- ⑦ Space velocity of the whole system = $\frac{V_0}{V_1 + V_2}$