

# Multiscale modeling of syndiospecific styrene polymerization

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**Abstract** A detailed mathematical model for syndiospecific styrene polymerization based on combining features of the multigrain model (MGM) and the polymeric multigrain model (PMGM). This model has been established to predict the radial monomer concentration within the growing macro particles and the rate of polymerization. The latter, the parameters, have an effect on the molecular weight distribution (MWD). In this model, the effect of intraparticle diffusion resistance and the radius of catalyst particles on the rate of polymerization and MWD were studied. The model simulation showed the presence of a large distribution of monomer concentration across the radius of particles. It was further noticed that the diffusion resistance was most intense at the beginning of the polymerization process. For MWD, the model simulation showed that the existence of diffusion resistance led to have an increase in the molecular weight within a period of time similar to the one needed in the catalyst decay. Moreover, the validation of the model with experimental data given a good agreement results and show that the model is able to predict a correct monomer profile, polymerization rate, particle growth factor and MWD, an algorithm, which embeds physicochemical effects, has been developed to model the industrial reactors.

**Keywords** Multiscale modeling · Particle growth · Multigrain model · Syndiospecific styrene polymerization · Mass transfer

## Nomenclature

$D_{ef,i}$	Effective macroparticle diffusivity, at the $i$ th grid point ( $\text{cm}^2 \cdot \text{min}^{-1}$ )
$D_1$	Monomer diffusivity in pure polymer ( $\text{cm}^2 \cdot \text{min}^{-1}$ )
$D_s$	Effective microparticle diffusion coefficient ( $\text{cm}^2 \cdot \text{min}^{-1}$ )
$k_p$	Propagation rate constant ( $\text{L} \cdot \text{mol}^{-1} \cdot \text{hr}^{-1}$ )
$k_d$	Catalyst deactivation rate constant ( $\text{hr}^{-1}$ )
$k_{tM}$	Chain transfer to monomer rate constant ( $\text{L} \cdot \text{mol}^{-1} \cdot \text{hr}^{-1}$ )
$k_{t\beta}$	$\beta$ —hydrogen elimination rate constant ( $\text{hr}^{-1}$ )
$k_l$	liquid film mass transfer coefficient ( $\text{m}^2 \cdot \text{s}^{-1}$ )
$M_{M,i}$	Monomer concentration in the macroparticle, at the $i$ th grid point ( $\text{mol} \cdot \text{dm}^{-3}$ )
$M_{\mu,i}$	Monomer concentration in the microparticle, at the $i$ th grid point ( $\text{mol} \cdot \text{dm}^{-3}$ )
$M_b$	Bulk monomer concentration ( $\text{mol} \cdot \text{dm}^{-3}$ )
$M_n$	Number average molecular weight ( $\text{g} \cdot \text{mol}^{-1}$ )
$M_w$	Weight average molecular weight ( $\text{g} \cdot \text{mol}^{-1}$ )
$(mw)_{sty}$	Styrene Molecular weight ( $\text{g} \cdot \text{mol}^{-1}$ )
$N$	Number of shell
$r$	Radial position at the macroparticle level (m)
$r_s$	Radial position at the microparticle level (m)
$R_c$	Radius of catalyst subparticles (m)
$R_{N+2}$	Macroparticle radius (m)
$R_o$	Initial particle radius (m)
$R_{h,i}$	Radius of $i$ th hypothetical shells
$R_{s,i}$	Radius of microparticle at $i$ th hypothetical shells
$R_{pv,i}$	Rate of reaction per unit volume at the $i$ th grid point ( $\text{mol} \cdot (\text{m}^3 \cdot \text{s})^{-1}$ )
$V_{cs,i}$	Volume of the $i$ th hypothesis shell
$V_{cc,i}$	Volume of catalyst in shell $i$

## Greek Letters

$\beta$	Indicator of the monomer convection contribution
$\lambda_{Pk}$	$k$ th Moment of live polymers
$\lambda_{Mk}$	$k$ th moment of dead polymers

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