



**Q3:** The elastic-rigid column ABCD shown in Fig. (3) has portion AB elastic while portion BCD rigid. Support A is hinge while support C is roller. The column is subjected to an axial compressive load (P) at the top end D as shown. For this column establish the following:

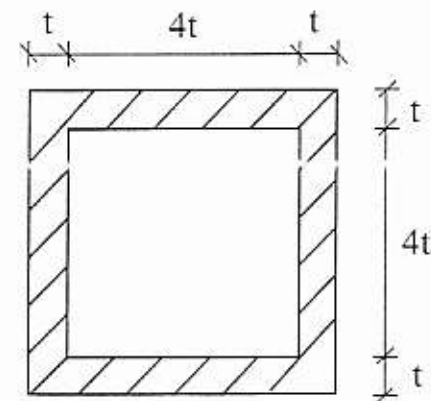
i) Starting from the second order differential equation  $EI \frac{d^2 v}{dx^2} = M(x)$ , derive an equation for the buckling load of the column.

ii) If the elastic portion AB of the column has the following properties;

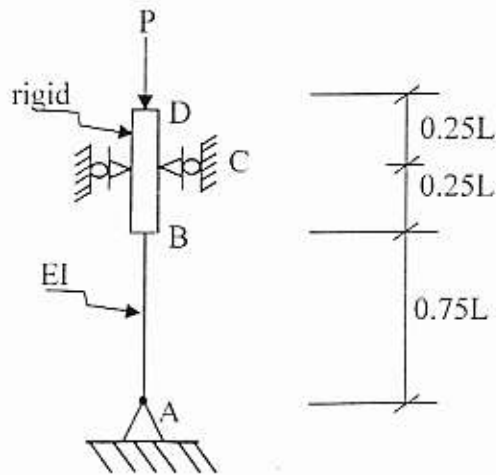
Hollow square cross section of dimensions shown in figure,

$L=3^m$ ,  $\sigma_y=250$  MPa,  $E=200 \times 10^3$  MPa,  $\frac{L}{r} = 160$  (slenderness ratio)

Find the dimension (t) of the column cross section, then find out whether the column fails by buckling or yielding.

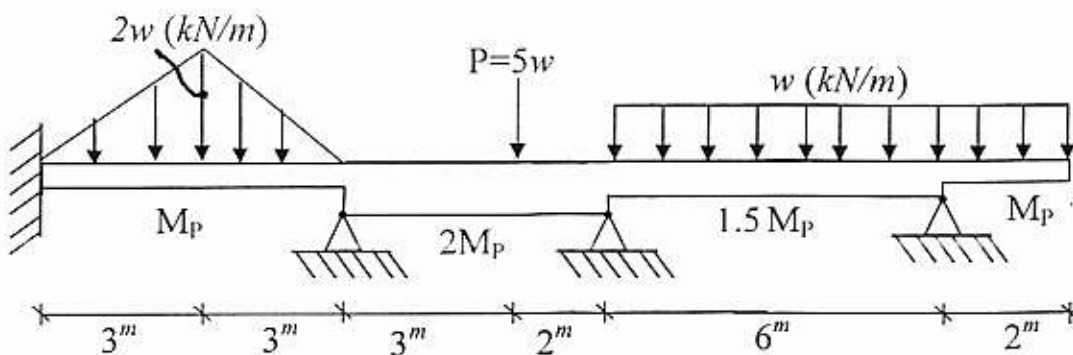


Cross section of column within portion AB



**Fig.(3)**

**Q4:** Using the plastic method of analysis, find the collapse load  $w_u$  (kN/m) of the continuous beam shown in Fig. (4).

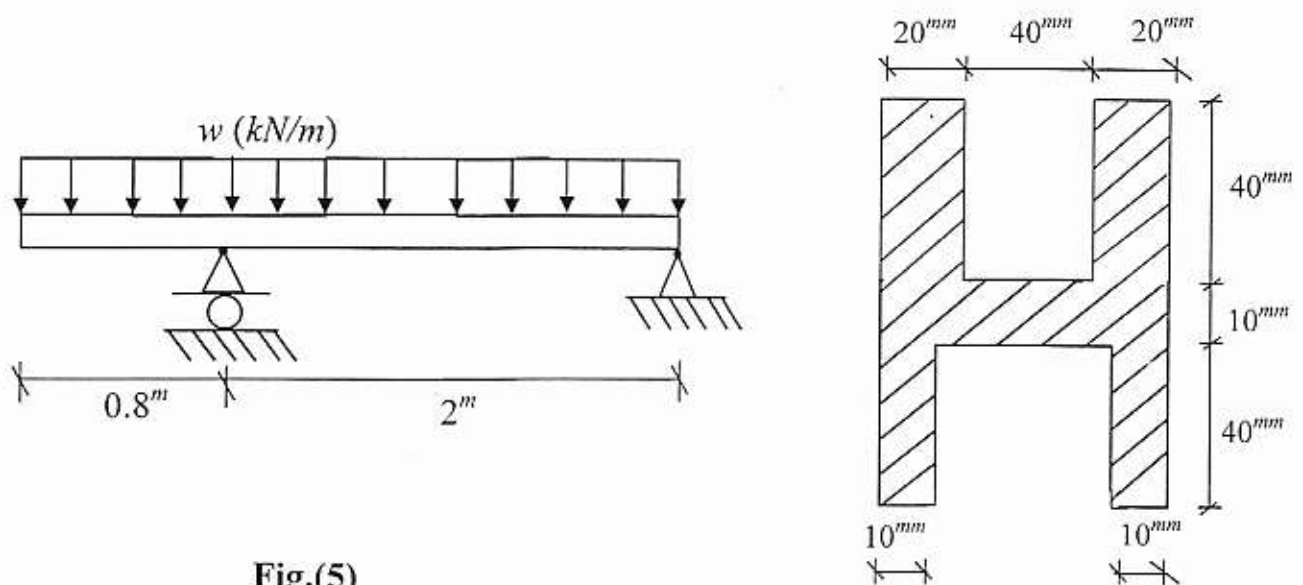


**Fig.(4)**

**Q5:** An overhang beam with H cross section is shown in Fig.(5) . The beam is subjected to an increasing uniformly distributed load  $w$  (kN/m) until fully plastic condition is reached.

Using  $\sigma_y = 250$  MPa ,

- Find the shape factor ( $\lambda$ ) of the beam cross section .
- Determine the limiting elastic uniform load  $w_y$  (kN/m).
- Determine the collapse uniform load  $w_u$  (kN/m).
- Sketch the collapse mechanism.



**Fig.(5)**

Cross section