



Subject: mathematics  
Branch: physics  
Examiner: Isra'a Hadi

Class: 3  
Time: 3 hours  
Date:

**Note: Answer 5 questions, 12 marks for each question.**

**Q1/** Use power series (up to five terms) to find the solution of the following differential equation:

$$(x^2 - 1)y'' + 3xy' + xy = 0$$

**Q2/** Is  $f(z) = 2xy + i(x^2 + y^2)$  analytic function or not? Where  $z$  is complex number and  $f(z)$  is complex function.

**Q3/** Find  $\int_1^{1.3} e^x + x \, dx$ , to three decimal places by Simpson (3/8) rule where  $N=3$ .

**Q4/** Solve the following Partial differential equation:

$$\frac{\partial u}{\partial x} = 3 \frac{\partial u}{\partial y} + \frac{1}{2} u$$

$$u(x,0) = 3e^{-5x} + 2e^{-3x}$$

**Q5/** Use Taylor method (up to 4 terms) at three decimal places to find  $y(0.2)$  where:

$$y' = x^2 + y \quad y(0) = 1 \quad , \quad h = 0.1$$

**Q6/** Evaluate the following integrals in terms of gamma and beta functions:

$$1) \int_0^{\infty} \frac{dy}{1 + y^4}$$

$$2) \int_0^2 y^{3/2} \left(1 - \frac{y}{2}\right)^4 dy$$

GOOD LUCK